



## SOUTHERN LEHIGH SCHOOL DISTRICT

5775 Main Street  
Center Valley, PA 18034

### Scope and Sequence for **Algebra I**

#### Standards for Mathematical Practice:

**MP1** Make sense of problems and persevere in solving them.  
**MP2** Reason abstractly and quantitatively.  
**MP3** Construct viable arguments and critique the reasoning of others.  
**MP4** Model with mathematics.

**MP5** Use appropriate tools strategically.  
**MP6** Attend to precision.  
**MP7** Look for and make use of structure.  
**MP8** Look for and express regularity in repeated reasoning.

#### N.RN – Number and Quantity – The Real Number System

CCSSM		PA Core Standards for Mathematics	
<b>Extend the properties of exponents to rational exponents.</b>  <b>N.RN.1</b> Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. <i>For example, we define <math>5^{\frac{1}{3}}</math> to be the cube root of 5 because we want <math>(5^{\frac{1}{3}})^3 = 5^{(\frac{1}{3})^3}</math> to hold, so <math>(5^{\frac{1}{3}})^3</math> must equal 5.</i>  <b>N.RN.2</b> Rewrite expressions involving radicals and rational exponents using the properties of exponents.		<b>CC.2.1.HS.F.1</b> Apply and extend the properties of exponents to solve problems with rational exponents.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 1 Operations and Linear Equations & Inequalities	
<b>A1.1.1 Operations with Real Numbers and Expressions</b>			
<b>A1.1.1.1</b> Represent and/or use numbers in equivalent forms (e.g., integers, fractions, decimals, percents, square roots, and exponents).		<b>A1.1.1.1.1</b> Compare and/or order any real numbers. Note: Rational and irrational may be mixed.	
		<b>A1.1.1.1.2</b> Simplify square roots.	
<b>A1.1.1.3</b> Use exponents, roots, and/or absolute values to solve problems.		<b>A1.1.1.3.1</b> Simplify/evaluate expressions involving properties/laws of exponents, roots, and/ or absolute values to solve problems. Note: Exponents should be integers from -10 to 10.	

## N.RN – Number and Quantity – The Real Number System – *Continued...*

CCSSM		PA Core Standards for Mathematics	
<b>Use properties of rational and irrational numbers.</b>  <b>N.RN.3</b> Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational.		<b>CC.2.1.HS.F.2</b> Apply properties of rational and irrational numbers to solve real world or mathematical problems.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 1 Operations and Linear Equations & Inequalities	
<b>A1.1.1 Operations with Real Numbers and Expressions</b>			
<b>A1.1.1.1</b> Represent and/or use numbers in equivalent forms (e.g., integers, fractions, decimals, percents, square roots, and exponents).		<b>A1.1.1.1.1</b> Compare and/or order any real numbers. Note: Rational and irrational may be mixed.	
		<b>A1.1.1.1.2</b> Simplify square roots.	
<b>A1.1.1.2</b> Apply number theory concepts to show relationships between real numbers in problem-solving settings.		<b>A1.1.1.2.1</b> Find the Greatest Common Factor (GCF) and/or the Least Common Multiple (LCM) for sets of monomials.	
<b>A1.1.1.3</b> Use exponents, roots, and/or absolute values to solve problems.		<b>A1.1.1.3.1</b> Simplify/evaluate expressions involving properties/laws of exponents, roots, and/ or absolute values to solve problems. Note: Exponents should be integers from -10 to 10.	
<b>A1.1.1.4</b> Use estimation strategies in problem solving situations.		<b>A1.1.1.4.1</b> Use estimation to solve problems.	

## N.Q – Number and Quantity – Quantities

CCSSM		PA Core Standards for Mathematics	
<b>Reason quantitatively and use units to solve problems.</b>  <b>N.Q.1</b> Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.  <b>N.Q.2</b> Define appropriate quantities for the purpose of descriptive modeling.  <b>N.Q.3</b> Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.		<b>CC.2.1.HS.F.3</b> Apply quantitative reasoning to choose and interpret units and scales in formulas, graphs and data displays.  <b>CC.2.1.HS.F.4</b> Use units as a way to understand problems and to guide the solution of multi-step problems.  <b>CC.2.1.HS.F.5</b> Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.  <b>CC.2.2.HS.D.9</b> Use reasoning to solve equations and justify the solution method.	
<b>Pennsylvania System of School Assessment (PSSA)</b>		M08.B-E Expressions and Equations	
<b>A1.1.2</b> Linear Equations			
<b>A1.1.2.1</b> Write, solve, and/or graph linear equations using various methods.		<b>A1.1.2.1.1</b> Write, solve, and/or apply a linear equation (including problem situations).	
		<b>A1.1.2.1.2</b> Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only.	
		<b>A1.1.2.1.3</b> Interpret solutions to problems in the context of the problem situation. Note: Linear equations only.	

## A.SSE – Algebra – Seeing Structure in Expressions

CCSSM		PA Core Standards for Mathematics	
<b>Interpret the structure of expressions.</b>  <b>A.SSE.1</b> Interpret expressions that represent a quantity in terms of its context. a. Interpret parts of an expression, such as terms, factors, and coefficients. b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret $P(1+r)^n$ as the product of $P$ and a factor not depending on $P$ .  <b>A.SSE.2</b> Use the structure of an expression to identify ways to rewrite it. <i>For example, see <math>x^4 - y^4</math> as <math>(x^2)^2 - (y^2)^2</math>, thus recognizing it as a difference of squares that can be factored as <math>(x^2 - y^2)(x^2 + y^2)</math>.</i>		<b>CC.2.2.HS.D.1</b> Interpret the structure of expressions to represent a quantity in terms of its context.	
<b>Write expressions in equivalent forms to solve problems.</b>  <b>A.SSE.3</b> Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. a. Factor a quadratic expression to reveal the zeros of the function it defines. b. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. c. Use the properties of exponents to transform expressions for exponential functions. <i>For example the expression <math>1.15^t</math> can be rewritten as <math>(1.15^{1/12})^{12t} \approx 1.012^{12t}</math> to reveal the approximate equivalent monthly interest rate if the annual rate is 15%</i>		<b>CC.2.2.HS.D.2</b> Write expressions in equivalent forms to solve problems.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 1 Operations and Linear Equations & Inequalities	
<b>A1.1.1 Operations with Real Numbers and Expressions</b>			
<b>A1.1.1.5</b> Simplify expressions involving polynomials.		<b>A1.1.1.5.1</b> Add, subtract, and/or multiply polynomial expressions (express answers in simplest form). Note: Nothing larger than a binomial multiplied by a trinomial.	
		<b>A1.1.1.5.2</b> Factor algebraic expressions, including difference of squares and trinomials. Note: Trinomials are limited to the form $ax^2+bx+c$ where $a$ is equal to 1 after factoring out all monomial factors.	
		<b>A1.1.1.5.3</b> Simplify/reduce a rational algebraic expression.	

## A.APR – Algebra – Arithmetic with Polynomials and Rational Expressions

CCSSM		PA Core Standards for Mathematics	
<b>Perform arithmetic operations on polynomials.</b>  <b>A.APR.1</b> Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.		<b>CC.2.2.HS.D.3</b> Extend the knowledge of arithmetic operations and apply to polynomials.  <b>CC.2.2.HS.D.5</b> Use polynomial identities to solve problems.  <b>CC.2.2.HS.D.6</b> Extend the knowledge of rational functions to rewrite in equivalent forms.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		<b>Module 1 Operations and Linear Equations &amp; Inequalities</b>	
<b>A1.1.1 Operations with Real Numbers and Expressions</b>			
<b>A1.1.1.5</b> Simplify expressions involving polynomials.		<b>A1.1.1.5.1</b> Add, subtract, and/or multiply polynomial expressions (express answers in simplest form). Note: Nothing larger than a binomial multiplied by a trinomial.	
		<b>A1.1.1.5.2</b> Factor algebraic expressions, including difference of squares and trinomials. Note: Trinomials are limited to the form $ax^2+bx+c$ where $a$ is equal to 1 after factoring out all monomial factors.	
		<b>A1.1.1.5.3</b> Simplify/reduce a rational algebraic expression.	

## A.CED – Algebra – Creating Equations

CCSSM		PA Core Standards for Mathematics	
<p><b>Create equations that describe numbers or relationships.</b></p> <p><b>A.CED.1</b> Create equations and inequalities in one variable and use them to solve problems. <i>Include equations arising from linear and quadratic functions, and simple rational</i></p> <p><b>A.CED.2</b> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.</p> <p><b>A.CED.3</b> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. <i>For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.</i></p> <p><b>A.CED.4</b> Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. <i>For example, rearrange Ohm's law <math>V = IR</math> to highlight resistance <math>R</math>.</i></p>		<p><b>CC.2.2.HS.D.7</b> Create and graph equations or inequalities to describe numbers or relationships.</p>	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 1 Operations and Linear Equations & Inequalities	
<b>A1.1.2 Linear Equations</b>			
<p><b>A1.1.2.1</b> Write, solve, and/or graph linear equations using various methods.</p>		<b>A1.1.2.1.1</b> Write, solve, and/or apply a linear equation (including problem situations).	
		<b>A1.1.2.1.2</b> Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only.	
		<b>A1.1.2.1.3</b> Interpret solutions to problems in the context of the problem situation. Note: Linear equations only.	
<p><b>A1.1.2.2</b> Write, solve, and/or graph systems of linear equations using various methods.</p>		<b>A1.1.2.2.1</b> Write and/or solve a system of linear equations (including problem situations) using graphing, substitution, and/or elimination. Note: Limit systems to two linear equations.	
		<b>A1.1.2.2.2</b> Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear equations.	
<p><b>A1.1.3.1</b> Write, solve, and/or graph linear inequalities using various methods.</p>		<b>A1.1.3.1.1</b> Write or solve compound inequalities and/or graph their solution sets on a number line (may include absolute value inequalities).	
		<b>A1.1.3.1.2</b> Identify or graph the solution set to a linear inequality on a number line.	
		<b>A1.1.3.1.3</b> Interpret solutions to problems in the context of the problem situation. Note: Limit to linear inequalities.	
<p><b>A1.1.3.2</b> Write, solve, and/or graph systems of linear inequalities using various methods.</p>		<b>A1.1.3.2.1</b> Write and/or solve a system of linear inequalities using graphing. Note: Limit systems to two linear inequalities.	
		<b>A1.1.3.2.2</b> Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear inequalities.	

## A.REI – Algebra – Reasoning with Equations & Inequalities

CCSSM	PA Core Standards for Mathematics
<p><b>Understand solving equations as a process of reasoning and explain the reasoning.</b></p> <p><b>A.REI.1</b> Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.</p>	<p><b>CC.2.2.HS.D.8</b> Apply inverse operations to solve equations or formulas for a given variable.</p> <p><b>CC.2.2.HS.D.9</b> Use reasoning to solve equations and justify the solution method.</p>
<p><b>Solve equations and inequalities in one variable.</b></p> <p><b>A.REI.3</b> Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.</p> <p><b>A.REI.4</b> Solve quadratic equations in one variable.</p> <ol style="list-style-type: none"> <li>Use the method of completing the square to transform any quadratic equation in <math>x</math> into an equation of the form <math>(x - p)^2 = q</math> that has the same solutions. Derive the quadratic formula from this form.</li> <li>Solve quadratic equations by inspection (e.g., for <math>x^2 = 49</math>), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as <math>a \pm bi</math> for real numbers <math>a</math> and <math>b</math>.</li> </ol> <p><b>Solve systems of equations.</b></p> <p><b>A.REI.5</b> Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.</p> <p><b>A.REI.6</b> Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.</p> <p><b>Represent and solve equations and inequalities graphically.</b></p> <p><b>A.REI.10</b> Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).</p> <p><i>This section continues on the next page...</i></p>	<p><b>CC.2.2.HS.D.10</b> Represent, solve and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically.</p> <p><i>This section continues on the next page...</i></p>

## A.REI – Algebra – Reasoning with Equations & Inequalities – *Continued...*

CCSSM		PA Core Standards for Mathematics	
<b>A.REI.3 – REI.6, AREI.10 <i>Continued...</i></b>  <b>A.REI.11</b> Explain why the $x$ -coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$ ; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.  <b>A.REI.12</b> Graph the solutions to a linear inequality in two variables as a half plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.		<b>CC.2.2.HS.D.10 <i>Continued...</i></b>	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 1 Operations and Linear Equations & Inequalities	
<b>A1.1.2 Linear Equations</b>			
<b>A1.1.2.1</b> Write, solve, and/or graph linear equations using various methods.		<b>A1.1.2.1.1</b> Write, solve, and/or apply a linear equation (including problem situations).	
		<b>A1.1.2.1.2</b> Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only.	
		<b>A1.1.2.1.3</b> Interpret solutions to problems in the context of the problem situation. Note: Linear equations only.	
<b>A1.1.2.2</b> Write, solve, and/or graph systems of linear equations using various methods.		<b>A1.1.2.2.1</b> Write and/or solve a system of linear equations (including problem situations) using graphing, substitution, and/or elimination. Note: Limit systems to two linear equations.	
		<b>A1.1.2.2.2</b> Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear equations.	
<b>A1.1.3.1</b> Write, solve, and/or graph linear inequalities using various methods.		<b>A1.1.3.1.1</b> Write or solve compound inequalities and/or graph their solution sets on a number line (may include absolute value inequalities).	
		<b>A1.1.3.1.2</b> Identify or graph the solution set to a linear inequality on a number line.	
		<b>A1.1.3.1.3</b> Interpret solutions to problems in the context of the problem situation. Note: Limit to linear inequalities.	
<b>A1.1.3.2</b> Write, solve, and/or graph systems of linear inequalities using various methods.		<b>A1.1.3.2.1</b> Write and/or solve a system of linear inequalities using graphing. Note: Limit systems to two linear inequalities.	
		<b>A1.1.3.2.2</b> Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear inequalities.	



## F.IF – Functions – Interpreting Functions

CCSSM	PA Core Standards for Mathematics
<p><b>Understand the concept of function and use function notation.</b></p> <p><b>F.IF.1</b> Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If <math>f</math> is a function and <math>x</math> is an element of its domain, then <math>f(x)</math> denotes the output of <math>f</math> corresponding to the input <math>x</math>. The graph of <math>f</math> is the graph of the equation <math>y = f(x)</math>.</p> <p><b>F.IF.2</b> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.</p> <p><b>F.IF.3</b> Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. <i><b>For example</b>, the Fibonacci sequence is defined recursively by <math>f(0) = f(1) = 1</math>, <math>f(n+1) = f(n) + f(n-1)</math> for <math>n \geq 1</math>.</i></p>	<p><b>CC.2.2.HS.C.1</b></p> <p>Use the concept and notation of functions to interpret and apply them in terms of their context.</p>
<p><b>Interpret functions that arise in applications in terms of the context.</b></p> <p><b>F.IF.4</b> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. <i>Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.</i></p> <p><b>F.IF.5</b> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. <i><b>For example</b>, if the function <math>h(n)</math> gives the number of person-hours it takes to assemble <math>n</math> engines in a factory, then the positive integers would be an appropriate domain for the function.</i></p> <p><b>F.IF.6</b> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.</p> <p><i>This section continues on the next page...</i></p>	<p><b>CC.2.2.HS.C.2</b></p> <p>Graph and analyze functions and use their properties to make connections between the different representations.</p> <p><i>This section continues on the next page...</i></p>

## F.IF – Functions – Interpreting Functions – *Continued...*

CCSSM	PA Core Standards for Mathematics
<p><b>F.IF.4 – F.IF.6 <i>Continued...</i></b></p> <p><b>Analyze functions using different representations.</b></p> <p><b>F.IF.7</b> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.</p> <ul style="list-style-type: none"> <li><b>a</b> Graph linear and quadratic functions and show intercepts, maxima, and minima.</li> <li><b>b</b> Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.</li> <li><b>c</b> Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.</li> </ul> <p><b>F.IF.8</b> Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.</p> <ul style="list-style-type: none"> <li><b>a</b> Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.</li> <li><b>b</b> Use the properties of exponents to interpret expressions for exponential functions. <b><i>For example, identify percent rate of change in functions such as <math>y = (1.02)^t</math>, <math>y = (0.97)^t</math>, <math>y = (1.01)^{12t}</math>, <math>y = (1.2)^{t/10}</math>, and classify them as representing exponential growth or decay.</i></b></li> </ul> <p><b>F.IF.9</b> Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <b><i>For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.</i></b></p> <p><i>This section continues on the next page...</i></p>	<p><b>CC.2.2.HS.C.2 <i>Continued...</i></b></p> <p><i>This section continues on the next page...</i></p>

## F.IF – Functions – Interpreting Functions – *Continued...*

CCSSM		PA Core Standards for Mathematics	
F.IF.4 – F.IF.9 <i>Continued...</i>		CC.2.2.HS.C.2 <i>Continued...</i>	
Pennsylvania System of School Assessment (Keystone)		Module 2 Linear Functions and Data Organization	
A1.2.1 Functions			
A1.2.1.1 Analyze and/or use patterns or relations.	A1.2.1.1.1 Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically.		
	A1.2.1.1.2 Determine whether a relation is a function, given a set of points or a graph.		
	A1.2.1.1.3 Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table).		
A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables.	A1.2.1.2.1 Create, interpret, and/or use the equation, graph, or table of a linear function.		
	A1.2.1.2.2 Translate from one representation of a linear function to another (i.e., graph, table, and equation).		
A1.2.2 Coordinate Geometry			
A1.2.2.1 Describe, compute, and/or use the rate of change (slope) of a line.	A1.2.2.1.1 Identify, describe, and/or use constant rates of change.		
	A1.2.2.1.2 Apply the concept of linear rate of change (slope) to solve problems.		
	A1.2.2.1.3 Write or identify a linear equation when given: the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point slope, standard, and/or slope-intercept form.		
	A1.2.2.1.4 Determine the slope and/or y-intercept represented by a linear equation or graph.		

## F.BF – Functions – Building Functions

CCSSM		PA Core Standards for Mathematics	
<b>Build a function that models a relationship between two quantities.</b>  <b>F.BF.1</b> Write a function that describes a relationship between two quantities. <b>a.</b> Determine an explicit expression, a recursive process, or steps for calculation from a context. <b>b.</b> Combine standard function types using arithmetic operations. <i>For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model.</i>  <b>F.BF.2</b> Write arithmetic sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.		<b>CC.2.2.HS.C.3</b> Write functions or sequences that model relationships between two quantities.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 1 Operations and Linear Equations & Inequalities	
<b>A1.1.2 Linear Equations</b>			
<b>A1.1.2.1</b> Write, solve, and/or graph linear equations using various methods.	<b>A1.1.2.1.1</b> Write, solve, and/or apply a linear equation (including problem situations).		
	<b>A1.1.2.1.2</b> Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only.		
	<b>A1.1.2.1.3</b> Interpret solutions to problems in the context of the problem situation. Note: Linear equations only.		
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 2 Linear Functions and Data Organization	
<b>A1.2.1 Functions</b>			
<b>A1.2.1.1</b> Analyze and/or use patterns or relations.	<b>A1.2.1.1.1</b> Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically.		
	<b>A1.2.1.1.2</b> Determine whether a relation is a function, given a set of points or a graph.		
	<b>A1.2.1.1.3</b> Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table).		
<b>A1.2.1.2</b> Interpret and/or use linear functions and their equations, graphs, or tables.	<b>A1.2.1.2.1</b> Create, interpret, and/or use the equation, graph, or table of a linear function.		
	<b>A1.2.1.2.2</b> Translate from one representation of a linear function to another (i.e., graph, table, and equation).		
<b>A1.2.2 Coordinate Geometry</b>			
<b>A1.2.2.1</b> Describe, compute, and/or use the rate of change (slope) of a line.	<b>A1.2.2.1.1</b> Identify, describe, and/or use constant rates of change.		
	<b>A1.2.2.1.2</b> Apply the concept of linear rate of change (slope) to solve problems.		
	<b>A1.2.2.1.3</b> Write or identify a linear equation when given: the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point slope, standard, and/or slope-intercept form.		
	<b>A1.2.2.1.4</b> Determine the slope and/or y-intercept represented by a linear equation or graph.		

## F.BF – Functions – Building Functions – *Continued...*

CCSSM		PA Core Standards for Mathematics	
<b>Build a new functions from existing functions.</b>  <b>F.BF.3</b> Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$ , $k f(x)$ , $f(kx)$ , and $f(x + k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. <i>Include recognizing even and odd functions from their graphs and algebraic expressions for them.</i>  <b>F.BF.4</b> Find inverse functions. <b>a.</b> Solve an equation of the form $f(x) = c$ for a simple function $f$ that has an inverse and write an expression for the inverse. <i>For example, <math>f(x) = 2x^3</math> or <math>f(x) = (x+1)/(x-1)</math> for <math>x \neq 1</math>.</i>		<b>CC.2.2.HS.C.4</b> Interpret the effects transformations have on functions and find the inverses of functions.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 2 Linear Functions and Data Organization	
<b>A1.2.1 Functions</b>			
<b>A1.2.1.2</b> Interpret and/or use linear functions and their equations, graphs, or tables.		<b>A1.2.1.2.1</b> Create, interpret, and/or use the equation, graph, or table of a linear function.	
		<b>A1.2.1.2.2</b> Translate from one representation of a linear function to another (i.e., graph, table, and equation).	

## F.LE – Functions – Linear, Quadratic, and Exponential Models

CCSSM		PA Core Standards for Mathematics	
<b>Construct and compare linear, quadratic, and exponential models and solve problems.</b> <b>F.LE.1</b> Distinguish between situations that can be modeled with linear functions and with exponential functions. <b>a.</b> Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals. <b>b.</b> Recognize situations in which one quantity changes at a constant rate per unit interval relative to another. <b>c.</b> Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.  <b>F.LE.2</b> Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).  <b>F.LE.3</b> Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.		<b>CC.2.2.HS.C.5</b> Construct and compare linear, quadratic and/or exponential models to solve problems.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 2 Linear Functions and Data Organization	
<b>A1.2.2 Coordinate Geometry</b>			
<b>A1.2.2.1</b> Describe, compute, and/or use the rate of change (slope) of a line.		<b>A1.2.2.1.1</b> Identify, describe, and/or use constant rates of change.	
		<b>A1.2.2.1.2</b> Apply the concept of linear rate of change (slope) to solve problems.	
		<b>A1.2.2.1.3</b> Write or identify a linear equation when given: the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point slope, standard, and/or slope-intercept form.	
		<b>A1.2.2.1.4</b> Determine the slope and/or y-intercept represented by a linear equation or graph.	
<b>Interpret expressions for functions in terms of the situation they model.</b>  <b>F.LE.5</b> Interpret the parameters in a linear or exponential function in terms of a context.		<b>CC.2.2.HS.C.6</b> Interpret functions in terms of the situation they model.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		Module 2 Linear Functions and Data Organization	
<b>A1.2.1 Functions</b>			
<b>A1.2.1.2</b> Interpret and/or use linear functions and their equations, graphs, or tables.		<b>A1.2.1.2.1</b> Create, interpret, and/or use the equation, graph, or table of a linear function.	
		<b>A1.2.1.2.2</b> Translate from one representation of a linear function to another (i.e., graph, table, and equation).	
<b>A1.2.2 Coordinate Geometry</b>			
<b>A1.2.2.2</b> Analyze and/or interpret data on a scatter plot.		<b>A1.2.2.2.1</b> Draw, identify, find, and/or write an equation for a line of best fit for a scatter plot.	

## S.ID – Statistics and Probability – Interpreting Categorical & Quantitative Data

CCSSM		PA Core Standards for Mathematics	
<b>Summarize, represent, and interpret data on a single count or measurement variable.</b>  <b>S.ID.1</b> Represent data with plots on the real number line (dot plots, histograms, and box plots).  <b>S.ID.2</b> Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.  <b>S.ID.3</b> Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).		<b>CC.2.4.HS.B.1</b> Summarize, represent, and interpret data on a single count or measurement variable.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		<b>Module 2 Linear Functions and Data Organization</b>	
<b>A1.2.2 Coordinate Geometry</b>			
<b>A1.2.2.1</b> Describe, compute, and/or use the rate of change (slope) of a line.		<b>A1.2.2.1.1</b> Identify, describe, and/or use constant rates of change.	
		<b>A1.2.2.1.2</b> Apply the concept of linear rate of change (slope) to solve problems.	
		<b>A1.2.2.1.3</b> Write or identify a linear equation when given: the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point slope, standard, and/or slope-intercept form.	
		<b>A1.2.2.1.4</b> Determine the slope and/or y-intercept represented by a linear equation or graph.	
<b>A1.2.3 Data Analysis</b>			
<b>A1.2.3.1</b> Use measures of dispersion to describe a set of data.		<b>A1.2.3.1.1</b> Calculate and/or interpret the range, quartiles, and interquartile range of data.	
<b>A1.2.3.2</b> Use data displays in problem-solving settings and/or to make predictions.		<b>A1.2.3.2.1</b> Estimate or calculate to make predictions based on a circle, line, bar graph, measures of central tendency, or other representations.	
		<b>A1.2.3.2.2</b> Analyze data, make predictions, and/or answer questions based on displayed data (box-and-whisker plots, stem-and-leaf plots, scatter plots, measures of central tendency, or other representations).	
		<b>A1.2.3.2.3</b> Make predictions using the equations or graphs of best-fit lines of scatter plots.	

## S.ID – Statistics and Probability – Interpreting Categorical & Quantitative Data – *Continued...*

CCSSM		PA Core Standards for Mathematics	
<b>Summarize, represent, and interpret data on two categorical and quantitative variables.</b>  <b>S.ID.5</b> Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.  <b>S.ID.6</b> Represent data on two quantitative variables on a scatter plot, and describe how the variables are related. <div><b>a.</b> Fit a function to the data; use functions fitted to data to solve problems in the context of the data. <i>Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.</i></div> <div><b>b.</b> Informally assess the fit of a function by plotting and analyzing residuals.</div> <div><b>c.</b> Fit a linear function for a scatter plot that suggests a linear association.</div>		<b>CC.2.4.HS.B.2</b> Summarize, represent, and interpret data on two categorical and quantitative variables.	
Pennsylvania System of School Assessment (Keystone)		Module 2 Linear Functions and Data Organization	
<b>A1.2.1 Functions</b>			
<b>A1.2.1.1</b> Analyze and/or use patterns or relations.		<b>A1.2.1.1.1</b> Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically.	
		<b>A1.2.1.1.2</b> Determine whether a relation is a function, given a set of points or a graph.	
		<b>A1.2.1.1.3</b> Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table).	
<b>A1.2.1.2</b> Interpret and/or use linear functions and their equations, graphs, or tables.		<b>A1.2.1.2.1</b> Create, interpret, and/or use the equation, graph, or table of a linear function.	
		<b>A1.2.1.2.2</b> Translate from one representation of a linear function to another (i.e., graph, table, and equation).	
<b>A1.2.2 Coordinate Geometry</b>			
<b>A1.2.2.2</b> Analyze and/or interpret data on a scatter plot.		<b>A1.2.2.2.1</b> Draw, identify, find, and/or write an equation for a line of best fit for a scatter plot.	



## S.ID – Statistics and Probability – Interpreting Categorical & Quantitative Data – *Continued...*

CCSSM		PA Core Standards for Mathematics	
<b>Interpret linear models.</b>  <b>S.ID.7</b> Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.  <b>S.ID.8</b> Compute (using technology) and interpret the correlation coefficient of a linear fit.  <b>S.ID.9</b> Distinguish between correlation and causation.		<b>CC.2.4.HS.B.3</b> Analyze linear models to make interpretations based on the data.  <b>CC.2.4.HS.B.5</b> Make inferences and justify conclusions based on sample surveys, experiments, and observational studies.	
<b>Pennsylvania System of School Assessment (Keystone)</b>		<b>Module 2 Linear Functions and Data Organization</b>	
<b>A1.2.2 Coordinate Geometry</b>			
<b>A1.2.2.2</b> Analyze and/or interpret data on a scatter plot.		<b>A1.2.2.1</b> Draw, identify, find, and/or write an equation for a line of best fit for a scatter plot.	
<b>A1.2.3 Data Analysis</b>			
<b>A1.2.3.1</b> Use measures of dispersion to describe a set of data.		<b>A1.2.3.1.1</b> Calculate and/or interpret the range, quartiles, and interquartile range of data.	
<b>A1.2.3.2</b> Use data displays in problem-solving settings and/or to make predictions.		<b>A1.2.3.2.1</b> Estimate or calculate to make predictions based on a circle, line, bar graph, measures of central tendency, or other representations.	
		<b>A1.2.3.2.2</b> Analyze data, make predictions, and/or answer questions based on displayed data (box-and-whisker plots, stem-and-leaf plots, scatter plots, measures of central tendency, or other representations).	
		<b>A1.2.3.2.3</b> Make predictions using the equations or graphs of best-fit lines of scatter plots.	

## S.CP – Statistics and Probability – Conditional Probability and Rules of Probability

CCSSM		PA Core Standards for Mathematics	
<p><b>Explain volume formulas and use them to solve problems.</b></p> <p><b>S.CP.1</b> Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events (“or,” “and,” “not”).</p> <p><b>S.CP.2</b> Understand that two events <math>A</math> and <math>B</math> are independent if the probability of <math>A</math> and <math>B</math> occurring together is the product of their probabilities, and use this characterization to determine if they are independent.</p> <p><b>S.CP.3</b> Understand the conditional probability of <math>A</math> given <math>B</math> as <math>P(A \text{ and } B)/P(B)</math>, and interpret independence of <math>A</math> and <math>B</math> as saying that the conditional probability of <math>A</math> given <math>B</math> is the same as the probability of <math>A</math>, and the conditional probability of <math>B</math> given <math>A</math> is the same as the probability of <math>B</math>.</p> <p><b>S.CP.4</b> Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. <i>For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results.</i></p> <p><b>S.CP.5</b> Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. <i>For example, compare the chance of having lung cancer if you are a smoker with the chance of being a smoker if you have lung cancer.</i></p>		<p><b>2.4.HS.B.6</b> Use the concepts of independence and conditional probability to interpret data.</p>	
<p><b>Use the rules of probability to compute probabilities of compound events.</b></p> <p><b>S.CP.6</b> Find the conditional probability of <math>A</math> given <math>B</math> as the fraction of <math>B</math>'s outcomes that also belong to <math>A</math>, and interpret the answer in terms of the model.</p> <p><b>S.CP.7</b> Apply the Addition Rule, <math>P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)</math>, and interpret the answer in terms of the model.</p>		<p><b>CC.2.4.HS.B.4</b> Recognize and evaluate random process underlying statistical experiments.</p> <p><b>CC.2.4.HS.B.7</b> Apply the rules of probability to compute probabilities of compound events in a uniform probability model.</p>	
<p><b>Pennsylvania System of School Assessment (Keystone)</b></p>		<p>Module 2 Linear Functions and Data Organization</p>	
<p><b>A1.2.3 Data Analysis</b></p>			
<p><b>A1.2.3.3</b> Apply probability to practical situations.</p>		<p><b>A1.2.3.3.1</b> Find probabilities for compound events (e.g., find probability of red and blue, find probability of red or blue) and represent as a fraction, decimal, or percent</p>	