



SOUTHERN LEHIGH SCHOOL DISTRICT

5775 Main Street
Center Valley, PA 18034

Scope and Sequence for **Grade 8 Mathematics**

Standards for Mathematical Practice:

MP1 Make sense of problems and persevere in solving them.
MP2 Reason abstractly and quantitatively.
MP3 Construct viable arguments and critique the reasoning of others.
MP4 Model with mathematics.

MP5 Use appropriate tools strategically.
MP6 Attend to precision.
MP7 Look for and make use of structure.
MP8 Look for and express regularity in repeated reasoning.

8.NS – The Number System

| CCSSM | PA Core Standards for Mathematics |
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| <p>Know that there are numbers that are not rational, and approximate them by rational numbers.</p> <p>8.NS.1 Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number.</p> <p>8.NS.2 Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., π^2). <i>For example, by truncating the decimal expansion of $\sqrt{2}$, show that $\sqrt{2}$ is between 1 and 2, then between 1.4 and 1.5, and explain how to continue on to get better approximations.</i></p> | <p>CC.2.1.8.E.1 Distinguish between rational and irrational numbers using their properties.</p> <p>CC.2.1.8.E.4 Estimate irrational numbers by comparing them to rational numbers.</p> |
| Pennsylvania System of School Assessment (PSSA) | |
| M08.A-N.1 Demonstrate an understanding of rational and irrational numbers | |
| <p>M08.A-N.1.1 Apply concepts of rational and irrational numbers.</p> | <p>M08.A-N.1.1.1 Determine whether a number is rational or irrational. For rational numbers, show that the decimal expansion terminates or repeats (limit repeating decimals to thousandths). M08.A-N.1.1.2 Convert a terminating or repeating decimal into a rational number (limit repeating decimals to thousandths). M08.A-N.1.1.3 Estimate the value of irrational numbers without a calculator (limit whole number radicand to less than 144). <i>Example: $\sqrt{5}$ is between 2 and 3 but closer to 2.</i> M08.A-N.1.1.4 Use rational approximations of irrational numbers to compare and order irrational numbers. M08.A-N.1.1.5 Locate/identify rational and irrational numbers at their approximate locations on a number line.</p> |

8.EE – Expressions and Equations

| CCSSM | | PA Core Standards for Mathematics | |
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| Expressions and Equations Work with radicals and integer exponents. 8.EE.1 Know and apply the properties of integer exponents to generate equivalent numerical expressions. <i>For example, $3^2 \times 3^{-5} = 3^{-3} = 1/3^3 = 1/27$.</i> 8.EE.2 Use square root and cube root symbols to represent solutions to equations of the form $x^2 = p$ and $x^3 = p$, where p is a positive rational number. Evaluate square roots of small perfect squares and cube roots of small perfect cubes. Know that $\sqrt{2}$ is irrational. 8.EE.3 Use numbers expressed in the form of a single digit times a whole-number power of 10 to estimate very large or very small quantities, and to express how many times as much one is than the other. <i>For example, estimate the population of the United States as 3 times 10^8 and the population of the world as 7 times 10^9, and determine that the world population is more than 20 times larger.</i> 8.EE.4 Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Use scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific notation that has been generated by technology. | | CC.2.2.8.B.1 Apply concepts of radicals and integer exponents to generate equivalent expressions. | |
| Pennsylvania System of School Assessment (PSSA) | | M08.B-E Expressions and Equations | |
| M08.B-E.1 Demonstrate an understanding of expressions and equations with radicals and integer exponents. | | | |
| M08.B-E.1.1 Represent and use expressions and equations to solve problems involving radicals and integer exponents. | | M08.B-E.1.1.1 Apply one or more properties of integer exponents to generate equivalent numerical expressions without a calculator (with final answers expressed in exponential form with positive exponents). Properties will be provided. <i>Example: $3^{12} \times 3^{-15} = 3^{-3} = 1/(3)^3$</i> | |
| | | M08.B-E.1.1.2 Use square root and cube root symbols to represent solutions to equations of the form $x^2 = p$ and $x^3 = p$, where p is a positive rational number. Evaluate square roots of perfect squares (up to and including 12^2) and cube roots of perfect cubes (up to and including 5^3) without a calculator. <i>Example: If $x^2 = 25$ then $x = \pm \sqrt{25}$.</i> | |
| | | M08.B-E.1.1.3 Estimate very large or very small quantities by using numbers expressed in the form of a single digit times an integer power of 10, and express how many times larger or smaller one number is than another. <i>Example: Estimate the population of the United States as 3×10^8 and the population of the world as 7×10^9, and determine that the world population is more than 20 times larger than the United States population.</i> | |
| | | M08.B-E.1.1.4 Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Express answers in scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific notation that has been generated by technology (e.g., interpret 4.7EE9 displayed on a calculator as 4.7×10^9). | |

8.EE – Expressions and Equations – *Continued...*

| CCSSM | | PA Core Standards for Mathematics | |
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| <p>Understand the connections between proportional relationships, lines, and linear equations.</p> <p>8.EE.5 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. For example, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed.</p> <p>8.EE.6 Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation $y = mx$ for a line through the origin and the equation $y = mx + b$ for a line intercepting the vertical axis at b.</p> | | <p>CC.2.2.8.B.2 Understand the connections between proportional relationships, lines, and linear equations.</p> | |
| <p>Pennsylvania System of School Assessment (PSSA)</p> | | <p>M08.B-E Expressions and Equations</p> | |
| <p>M08.B-E.2 Understand the connections between proportional relationships, lines, and linear equations.</p> | | | |
| <p>M08.B-E.2.1 Analyze and describe linear relationships between two variables, using slope.</p> | | <p>M08.B-E.2.1.1 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. <i>Example: Compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed.</i></p> | |
| | | <p>M08.B-E.2.1.2 Use similar right triangles to show and explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane.</p> | |
| | | <p>M08.B-E.2.1.3 Derive the equation $y = mx$ for a line through the origin and the equation $y = mx + b$ for a line intercepting the vertical axis at b.</p> | |
| <p>Analyze and solve linear equations and pairs of simultaneous linear equations.</p> <p>8.EE.7 Solve linear equations in one variable.</p> <p>a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form $x = a$, $a = a$, or $a = b$ results (where a and b are different numbers).</p> <p>b. Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.</p> <p><i>This section continues on the next page...</i></p> | | <p>CC.2.2.8.B.3 Analyze and solve linear equations and pairs of simultaneous linear equations.</p> <p><i>This section continues on the next page...</i></p> | |

8.EE – Expressions and Equations – *Continued...*

| CCSSM | PA Core Standards for Mathematics |
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| <p>8.EE.7 <i>Continued...</i></p> <p>8.EE.8 Analyze and solve pairs of simultaneous linear equations.</p> <p>a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</p> <p>b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. <i>For example, $3x + 2y = 5$ and $3x + 2y = 6$ have no solution because $3x + 2y$ cannot simultaneously be 5 and 6.</i></p> <p>c. Solve real-world and mathematical problems leading to two linear equations in two variables. <i>For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.</i></p> | <p>CC.2.2.8.B.3<i>Continued...</i></p> |
| Pennsylvania System of School Assessment (PSSA) | |
| M08.B-E.3 Analyze and solve linear equations and pairs of simultaneous linear equations. | |
| <p>M08.B-E.3.1 Write, solve, graph, and interpret linear equations in one or two variables, using various methods.</p> | <p>M08.B-E.3.1.1 Write and identify linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form $x = a$, $a = a$, or $a = b$ results (where a and b are different numbers).</p> |
| | <p>M08.B-E.3.1.2 Solve linear equations that have rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.</p> |
| | <p>M08.B-E.3.1.3 Interpret solutions to a system of two linear equations in two variables as points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</p> |
| | <p>M08.B-E.3.1.4 Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. <i>Example: $3x + 2y = 5$ and $3x + 2y = 6$ have no solution because $3x + 2y$ cannot simultaneously be 5 and 6.</i></p> |
| | <p>M08.B-E.3.1.5 Solve real-world and mathematical problems leading to two linear equations in two variables. <i>Example: Given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.</i></p> |

8.F – Functions

| CCSSM | | PA Core Standards for Mathematics | |
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| Define, evaluate, and compare functions. 8.F.1 Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output. 8.F.2 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <i>For example, given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change.</i> 8.F.3 Interpret the equation $y = mx + b$ as defining a linear function, whose graph is a straight line; give examples of functions that are not linear. <i>For example, the function $A = s^2$ giving the area of a square as a function of its side length is not linear because its graph contains the points (1,1), (2,4) and (3,9), which are not on a straight line.</i> | | CC.2.2.8.C.1 Define, evaluate, and compare functions. | |
| Pennsylvania System of School Assessment (PSSA) | | M08.B-F Functions | |
| M08.B-F.1 Analyze and interpret functions. | | | |
| M08.B-F.1.1 Define, evaluate, and compare functions displayed algebraically, graphically, numerically in tables, or by verbal descriptions. | | M08.B-F.1.1.1 Determine whether a relation is a function. | |
| | | M08.B-F.1.1.2 Compare properties of two functions each represented in a different way (i.e., algebraically, graphically, numerically in tables, or by verbal descriptions). <i>Example: Given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change.</i> | |
| | | M08.B-F.1.1.3 Interpret the equation $y = mx + b$ as defining a linear function whose graph is a straight line; give examples of functions that are not linear. | |
| Use functions to model relationships between quantities. 8.F.4 Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values. 8.F.5 Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally. | | CC.2.2.8.C.2 Use concepts of functions to model relationships between quantities. | |
| <i>This section continues on the next page...</i> | | <i>This section continues on the next page...</i> | |

| CCSSM | | PA Core Standards for Mathematics | |
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| 8.F.4, 8.F.5 <i>Continued...</i> | | CC.2.2.8.C.2 <i>Continued...</i> | |
| Pennsylvania System of School Assessment (PSSA) | | M08.B-F Functions | |
| M08.B-F.2 Use functions to model relationships between quantities. | | | |
| M08.B-F.2.1 Represent or interpret functional relationships between quantities using tables, graphs, and descriptions. | | M08.B-F.2.1.1 Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models and in terms of its graph or a table of values. | |
| | | M08.B-F.2.1.2 Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch or determine a graph that exhibits the qualitative features of a function that has been described verbally. | |

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8.G – Geometry – *Continued...*

| CCSSM | | PA Core Standards for Mathematics | |
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| 8.G.1 , 8.G.2, 8.G.3, 8.G.4 <i>Continued...</i> 8.G.5 Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. <i>For example, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so</i> | | CC.2.3.8.A.2 <i>Continued...</i> | |
| Pennsylvania System of School Assessment (PSSA) | | M08.C-G Geometry | |
| M08.C-G.1 Demonstrate an understanding of geometric transformations. | | | |
| M08.C-G.1.1 Apply properties of geometric transformations to verify congruence or similarity. | | M08.C-G.1.1.1 Identify and apply properties of rotations, reflections, and translations. <i>Example: Angle measures are preserved in rotations, reflections, and translations.</i> | |
| | | M08.C-G.1.1.2 Given two congruent figures, describe a sequence of transformations that exhibits the congruence between them. | |
| | | M08.C-G.1.1.3 Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures, using coordinates. | |
| | | M08.C-G.1.1.4 Given two similar two-dimensional figures, describe a sequence of transformations that exhibits the similarity between them. | |
| Understand and apply the Pythagorean Theorem. 8.G.6 Explain a proof of the Pythagorean Theorem and its converse. 8.G.7 Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions. 8.G.8 Apply the Pythagorean Theorem to find the distance between two points in a coordinate system. | | CC.2.3.8.A.3 Understand and apply the Pythagorean Theorem to solve problems. | |
| Pennsylvania System of School Assessment (PSSA) | | M08.C-G Geometry | |
| M08.C-G.1 Demonstrate an understanding of geometric transformations. | | | |
| M08.C-G.2.1 Solve problems involving right triangles by applying the Pythagorean theorem. | | M08.C-G.2.1.1 Apply the converse of the Pythagorean theorem to show a triangle is a right triangle. | |
| | | M08.C-G.2.1.2 Apply the Pythagorean theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions. (Figures provided for problems in three dimensions will be consistent with Eligible Content in grade 8 and below.) | |
| | | M08.C-G.2.1.3 Apply the Pythagorean theorem to find the distance between two points in a coordinate system. | |

8.G – Geometry – *Continued...*

| CCSSM | | PA Core Standards for Mathematics | |
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| <p>Solve real-world and mathematical problems involving volume of cylinders, cones, and spheres.</p> <p>8.G.9 Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.</p> | | <p>CC.2.3.8.A.1 Apply the concepts of volume of cylinders, cones, and spheres to solve real-world and mathematical problems.</p> | |
| Pennsylvania System of School Assessment (PSSA) | | M08.C-G Geometry | |
| M08.C-G.3 Solve real-world and mathematical problems involving volume. | | | |
| <p>M08.C-G.3.1 Apply volume formulas of cones, cylinders, and spheres.</p> | | <p>M08.C-G.3.1.1 Apply formulas for the volumes of cones, cylinders, and spheres to solve real-world and mathematical problems. <i>Formulas will be provided.</i></p> | |

CCSSM PA Core Standards for Mathematics

PA Core Standards for Mathematics

CC.2.4.8.B.1

Analyze and/or interpret bivariate data displayed in multiple representations.

CC.2.4.8.B.2

Understand that patterns of association can be seen in bivariate data utilizing frequencies.

M08.D-S Statistics and Probability

M08.D-S.1 Investigate patterns of association in bivariate data.

M08.D-S.1.1.1 Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative correlation, linear association, and nonlinear association.

M08.D-S.1.1.2 For scatter plots that suggest a linear association, identify a line of best fit by judging the closeness of the data points to the line.

M08.D-S.1.1.3 Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept.
Example: *In a linear model for a biology experiment, interpret a slope of 1.5 cm/hr as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height.*

M08.D-S.1.2.1 Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible associations between the two variables.
Example: Given data on whether students have a curfew on school nights and whether they have assigned chores at home, is there evidence that those who have a curfew also tend to have chores?

Scope and Sequence for Grade 8 Mathematics

Board Reviewed April 2019